

# Measurements of Heavy Meson Lifetimes with Belle

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## Abstract

Charmed and beauty meson lifetimes have been measured using  $2.75 \text{ fb}^{-1}$  ( $D$  mesons) and  $5.1 \text{ fb}^{-1}$  ( $B$  mesons) of data collected with the Belle detector at KEKB. The results are  $\tau(\overline{B}^0) = (1.50 \pm 0.05 \pm 0.07) \text{ ps}$ ,  $\tau(B^-) = (1.70 \pm 0.06^{+0.11}_{-0.10}) \text{ ps}$ ,  $\tau(D^0) = (414.8 \pm 3.8 \pm 3.4) \text{ fs}$ ,  $\tau(D^+) = (1040^{+23}_{-22} \pm 18) \text{ fs}$  and  $\tau(D_s^+) = (479^{+17+6}_{-16-8}) \text{ fs}$ , where the first error is statistical and the second error is systematic. The lifetime ratios are measured to be  $\tau(B^-)/\tau(\overline{B}^0) = 1.14 \pm 0.06^{+0.06}_{-0.05}$ ,  $\tau(D^+)/\tau(D^0) = 2.51 \pm 0.06 \pm 0.04$  and  $\tau(D_s^+)/\tau(D^0) = 1.15 \pm 0.04^{+0.01}_{-0.02}$ . The mixing parameter  $y_{CP}$  is also measured to be  $y_{CP} = 0.03^{+0.15+0.05}_{-0.18-0.08}$  for  $\overline{B}^0$  and  $y_{CP} = (1.0^{+3.8+1.1}_{-3.5-2.1})\%$  for  $D^0$ , corresponding to 95% confidence intervals,  $-0.36 < y_{CP} < 0.35$  and  $-7.0\% < y_{CP} < 8.7\%$ , respectively. All results are preliminary.

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Measurements of individual heavy meson lifetimes provide useful information for the theoretical understanding of heavy meson decay mechanisms. In particular, experimental results[1] yield  $\tau(D_s^+)/\tau(D^0) = 1.191 \pm 0.024$ , which is inconsistent with the theoretically expected range[2] of 1.00–1.07. Moreover, measurements of the differences of lifetimes for neutral mesons decaying into CP-mixed states and CP-eigenstates can be used to study the  $y \equiv \Delta\Gamma/2\Gamma$  and  $x \equiv \Delta M/\Gamma$  particle-antiparticle mixing parameters.

The parameter  $y_{CP}$ , defined as

$$y_{CP} \equiv \frac{\Gamma(\text{CP even}) - \Gamma(\text{CP odd})}{\Gamma(\text{CP even}) + \Gamma(\text{CP odd})}$$

is related to  $y$  and  $x$  by the expression

$$\begin{aligned} y_{CP} &= \frac{\tau(D^0 \rightarrow K^- \pi^+)}{\tau(D^0 \rightarrow K^- K^+)} - 1 \\ &\approx y \cos \phi - \frac{A_{mix}}{2} x \sin \phi, \\ y_{CP} &= 1 - \frac{\tau(\bar{B}^0 \rightarrow D^{*+} \ell^- \bar{\nu}, \bar{B}^0 \rightarrow D \pi)}{\tau(\bar{B}^0 \rightarrow J/\psi K_S)} \\ &\approx y \cos 2\phi_1, \end{aligned}$$

where  $\phi(\phi_1)$  is a CP-violating weak phase due to the interference of decays with and without mixing, and  $A_{mix}$  is a state-mixing CP-violating parameter ( $A_{mix} \approx 4\mathcal{R}e(\epsilon)$ ). The FOCUS experiment reports  $y_{CP} = (3.42 \pm 1.39 \pm 0.74)\%$ [3], while CLEO gives  $y' \cos \phi = (-2.5_{-1.6}^{+1.4})\%$ [4],  $x' = (0.0 \pm 1.5 \pm 0.2)\%$  and  $A_{mix} = 0.23_{-0.80}^{+0.63}$  using  $D^0 \rightarrow K^+ \pi^-$ , where  $y' = y \cos \delta - x \sin \delta$  and  $x' = x \cos \delta + y \sin \delta$ ;  $\delta$  is a strong phase between  $D^0 \rightarrow K^+ \pi^-$  and  $\bar{D}^0 \rightarrow K^+ \pi^-$  decays. These results may be an indication of a large  $SU(3)$ -breaking effect in  $D^0 \rightarrow K^\pm \pi^\mp$  decays[5].

This report mainly describes the  $\bar{B} \rightarrow D^* \ell^- \bar{\nu}$  analysis. The  $D$  lifetime analyses are described in Ref. 6.

Candidate  $\bar{B} \rightarrow D^* \ell^- \bar{\nu}$  decays are selected by applying kinematic constraints on events with a lepton and a  $D^* \rightarrow D^0 \pi$  decay chain, where  $D^0 \rightarrow K^- \pi^+$ ,  $K^- \pi^+ \pi^0$  and  $K^- \pi^+ \pi^+ \pi^-$  decays are used. First, the  $D^0$  decay vertex is determined and then the decay vertex of the  $\bar{B} \rightarrow D^* \ell^- \bar{\nu}$  candidate is calculated using the lepton and the inferred  $D^0$  track. The vertex point of the accompanying  $B$  meson is determined from the remaining tracks, after the rejection of  $K_S$  daughters and badly measured tracks. When the reduced  $\chi^2$  of the vertex fit is worse than 20, the track that gives the largest contribution to the  $\chi^2$  is removed and the vertex fit is repeated. This procedure is iterated until the  $\chi^2$  requirement is satisfied. Since the method does not properly treat displaced charm

vertices and their daughter tracks, a degradation of the vertex resolution and a bias on the vertex position is introduced. An interaction point constraint is applied to the vertex fit for both  $B$  mesons in order to improve the vertex resolution. The typical  $\Delta z$  resolution is 100  $\mu\text{m}$ . The proper-time difference is approximated as  $\Delta t \approx \Delta z/c(\beta\gamma)_\Upsilon$  where  $(\beta\gamma)_\Upsilon$  is  $\beta\gamma$  of the  $\Upsilon(4S)$  in the laboratory frame.

The likelihood function for  $\bar{B} \rightarrow D^* \ell^- \bar{\nu}$  lifetime fit is defined as

$$\begin{aligned} L(\tau_0, \tau_-, S_t, f_t, S_{BG}, \mu_{BG}, \lambda_{BG}, f_{\lambda BG}) \\ = \prod_i \int_{-\infty}^{\infty} d(\Delta t') [p_{SIG}^i(\Delta t') + p_{BG}^i(\Delta t')], \\ p_{SIG}^i(\Delta t') = (f_0^i \frac{e^{-\frac{|\Delta t'|}{\tau_0}}}{2 \cdot \tau_0} + f_-^i \frac{e^{-\frac{|\Delta t'|}{\tau_-}}}{2 \cdot \tau_-}) \\ [(1 - f_t) \frac{e^{-\frac{(\Delta t_i - \Delta t' - \mu)^2}{2\sigma_i^2}}}{\sqrt{2\pi}\sigma_i} + f_t \frac{e^{-\frac{(\Delta t_i - \Delta t' - \mu_t)^2}{2(\sigma_t^i)^2}}}{\sqrt{2\pi}\sigma_t^i}], \\ p_{BG}^i(\Delta t') = \sum_k f_k^i \frac{e^{-\frac{(\Delta t_i - \Delta t' - \mu_{BG}^k)^2}{2(S_{BG}^k \sigma_i)^2}}}{\sqrt{2\pi}S_{BG} \sigma_i} \\ [(1 - f_{\lambda BG}^k) \cdot \delta(\Delta t') + f_{\lambda BG}^k \frac{\lambda_{BG}^k}{2} e^{-\lambda_{BG}^k |\Delta t'|}], \end{aligned}$$

where:  $\tau_0$  and  $\tau_-$  are the  $\bar{B}^0$  and  $B^-$  lifetimes;  $\sigma_i$  and  $\sigma_t^i$  are the main and tail parts of the  $\Delta t$  resolution calculated event-by-event from the track error matrix as described below;  $f_t$  denotes the fraction of the tail part of the signal resolution function and is determined from the fit.  $\mu$  and  $\mu_t$  are the biases due to the charm meson daughter tracks, determined from the MC simulation;  $S_{BG}$ ,  $\mu_{BG}^k$ ,  $\lambda_{BG}^k$ ,  $f_{\lambda BG}^k$  are background-shape parameters, determined from the fit (fake  $D^*$ ), data (fake lepton) or MC (random  $D^* \ell$ );  $f_0^i$ ,  $f_-^i$  and  $f_k^i$  are fractions of the  $\bar{B}^0$  and  $B^-$  signals and background contributions that are calculated event-by-event using the measured  $\Delta M_{D^*}$  value. The  $\bar{B} \rightarrow D^* X \ell^- \bar{\nu}$  background fractions are estimated from the known branching fractions and included in  $f_0^i$  and  $f_-^i$ , since the effect of the missing  $X$  is found to be negligible.

The  $\Delta t$  resolution is a convolution of the  $\Delta z$  resolution and the error due to the kinematic approximation ( $\Delta t \approx \Delta z/c(\beta\gamma)_\Upsilon$ )  $\sigma_K$ :

$$\sigma_i^2 = [\sigma_{\Delta z}/c(\beta\gamma)_\Upsilon]^2 + \sigma_K^2.$$

The  $\Delta z$  resolution  $\sigma_{\Delta z}$  is calculated from the vertex resolutions of the reconstructed ( $\sigma_z^{rec}$ ) and associated ( $\sigma_z^{asc}$ )  $B$  mesons:

$$\sigma_{\Delta z}^2 = (S_{det} \sigma_z^{rec})^2 + (S_{det}^2 + S_{charm}^2)(\sigma_z^{asc})^2,$$

where  $S_{det}$  is a global scaling factor that accounts for any systematic bias in the resolution calculation from the track-helix errors, and  $S_{charm}$  is a scaling factor to account for the degradation of the vertex resolution of the associated  $B$  meson due to contamination of charm daughters. If the reduced  $\chi^2$  ( $\chi^2/n$ ) of the vertex fit is worse than 3, the corresponding vertex error ( $\sigma_z^{rec}$  or  $\sigma_z^{asc}$ ) is scaled by  $[1 + \alpha(\chi^2/n - 3)]$ . This  $\chi^2/n$ -dependent scaling is essential to account for events with large errors. We use the value of  $S_{det} = 0.99 \pm 0.04$  determined from the  $D^0$  lifetime fit in the  $z$  direction. The values for  $\sigma_K$ ,  $S_{charm}$  and  $\alpha$  are determined from the MC.  $\sigma_i^i$  is calculated in a similar manner. The associated parameter  $S_t$  is determined in the fit along with  $f_t$ . Figure 1 shows the  $\Delta t_{rec} - \Delta t_{gen}$  distribution and resolution function for MC signal events.

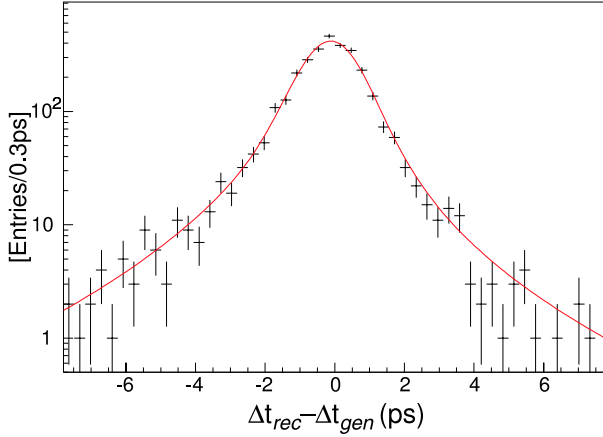


Figure 1: The  $\Delta t_{rec} - \Delta t_{gen}$  distribution and resolution function for MC signal events.

The likelihood function for the hadronic modes is defined as

$$\begin{aligned}
L(\tau_{sig}, S_{BG}, S_t^{BG}, \mu_{BG}, \mu_t^{BG}, f_t^{BG}, \lambda_{BG}, f_{\lambda BG}) \\
= \prod_i \int_{-\infty}^{\infty} d(\Delta t') [p_{SIG}^i(\Delta t') + p_{BG}^i(\Delta t')], \\
p_{SIG}^i(\Delta t') = (1 - f_{BG}^i) \frac{e^{-\frac{|\Delta t'|}{\tau_{sig}}}}{2 \cdot \tau_{sig}} \\
[(1 - f_t) \frac{e^{-\frac{(\Delta t_i - \Delta t' - \mu)^2}{2\sigma_i^2}}}{\sqrt{2\pi}\sigma_i} + f_t \frac{e^{-\frac{(\Delta t_i - \Delta t' - \mu_t)^2}{2(\sigma_t^{BG})^2}}}{\sqrt{2\pi}\sigma_t^i}], \\
p_{BG}^i(\Delta t') = f_{BG}^i (1 - f_t^{BG}) \frac{e^{-\frac{(\Delta t_i - \Delta t' - \mu_{BG})^2}{2(S_{BG}\sigma_i)^2}}}{\sqrt{2\pi}S_{BG}\sigma_i} \\
+ f_t^{BG} \frac{e^{-\frac{(\Delta t_i - \Delta t' - \mu_t^{BG})^2}{2(S_t^{BG}\sigma_i)^2}}}{\sqrt{2\pi}S_t^{BG}\sigma_i}
\end{aligned}$$

$$[(1 - f_{\lambda BG}) \cdot \delta(\Delta t') + f_{\lambda BG} \frac{\lambda_{BG}}{2} e^{-\lambda_{BG}|\Delta t'|}].$$

The fraction of background  $f_{BG}^i$  is calculated from the  $\Delta E$  and  $M_b$  values for each event. The background shape parameters  $S_{BG}$ ,  $S_t^{BG}$ ,  $\mu_{BG}$ ,  $\mu_t^{BG}$ ,  $f_t^{BG}$ ,  $\lambda_{BG}$  and  $f_{\lambda BG}$  are determined from the fit. We use  $S_{det} = 0.94 \pm 0.04$  in the  $\bar{B} \rightarrow J/\psi K$  analysis to account for slightly different kinematic properties from  $\bar{B} \rightarrow D^* \ell^- \bar{\nu}$ ,  $D\pi$  decays.

Figure 2 shows the  $\Delta t$  distributions and fit results for  $\bar{B}^0 \rightarrow D^{*+} \ell^- \bar{\nu}$  and  $B^- \rightarrow J/\psi K^-$  events. Table 1 summarizes the measurement results. The main sources of systematic errors are uncertainties in the resolution function and the  $\Delta t$  dependence of the reconstruction efficiency. All results are preliminary.

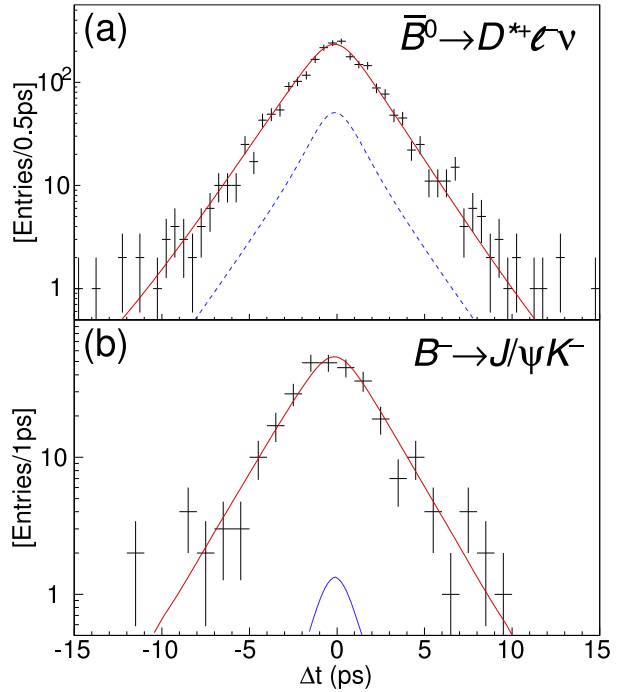


Figure 2: The  $\Delta t$  distributions and fit results for (a)  $\bar{B}^0 \rightarrow D^{*+} \ell^- \bar{\nu}$  and (b)  $B^- \rightarrow J/\psi K^-$  events. The dotted curve represents the background.

Table 1: Summary of lifetime measurements.

(a)  $B$  lifetime measurements.

$\overline{B}^0 \rightarrow D^{*+} \ell^- \overline{\nu}$	$(1.50 \pm 0.06^{+0.06}_{-0.04})$ ps
$\overline{B}^0 \rightarrow D^{*+} \pi^-$	$(1.55^{+0.18+0.10}_{-0.17-0.07})$ ps
$\overline{B}^0 \rightarrow D^+ \pi^-$	$(1.41^{+0.13}_{-0.12} \pm 0.07)$ ps
$\overline{B}^0 \rightarrow J/\psi \overline{K}^{*0}$	$(1.56^{+0.22+0.09}_{-0.19-0.15})$ ps
$\overline{B}^0$ combined	$(1.50 \pm 0.05 \pm 0.07)$ ps
$\overline{B}^0 \rightarrow J/\psi K_S$	$(1.54^{+0.28+0.11}_{-0.24-0.19})$ ps
$B^- \rightarrow D^{*0} \ell^- \overline{\nu}$	$(1.54 \pm 0.10^{+0.14}_{-0.07})$ ps
$B^- \rightarrow D^0 \pi^-$	$(1.73 \pm 0.10 \pm 0.09)$ ps
$B^- \rightarrow J/\psi K^-$	$(1.87^{+0.13+0.07}_{-0.12-0.14})$ ps
$B^-$ combined	$(1.70 \pm 0.06^{+0.11}_{-0.10})$ ps
$\tau(B^-)/\tau(\overline{B}^0)$	$1.14 \pm 0.06^{+0.06}_{-0.05}$
$y_{CP}$	$0.03^{+0.15+0.05}_{-0.18-0.08}$

(b)  $D$  lifetime measurements.

$D^0 \rightarrow K^- \pi^+$	$(414.8 \pm 3.8 \pm 3.4)$ fs
$D^0 \rightarrow K^- K^+$	$(410.5 \pm 14.3^{+9.7}_{-5.9})$ fs
$D^+ \rightarrow K^- \pi^+ \pi^+$	$(1049^{+25+16}_{-24-19})$ fs
$D^+ \rightarrow \phi \pi^+$	$(974^{+68+26}_{-62-18})$ fs
$D^+$ combined	$(1040^{+23}_{-22} \pm 18)$ fs
$D_s^+ \rightarrow \phi \pi^+$	$(470 \pm 19^{+5}_{-7})$ fs
$D_s^+ \rightarrow \overline{K}^{*0} K^+$	$(505^{+34+8}_{-33-12})$ fs
$D_s^+$ combined	$(479^{+17+6}_{-16-8})$ fs
$\tau(D^+)/\tau(D^0)$	$2.51 \pm 0.06 \pm 0.04$
$\tau(D_s^+)/\tau(D^0)$	$1.15 \pm 0.04^{+0.01}_{-0.02}$
$y_{CP}$	$(1.0^{+3.8+1.1}_{-3.5-2.1})\%$

## References

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